

# 1.1 Identify Points, Lines, and Planes



**Before**

You studied basic concepts of geometry.

**Now**

You will name and sketch geometric figures.

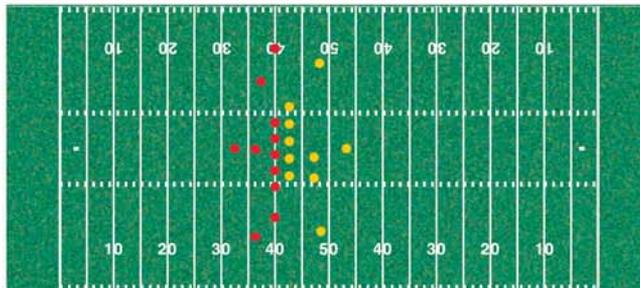
**Why**

So you can use geometry terms in the real world, as in Ex. 13.

## Key Vocabulary

- **undefined terms**  
point, line, plane
- **collinear points**
- **coplanar points**
- **defined terms**
- **line segment**
- **endpoints**
- **ray**
- **opposite rays**
- **intersection**

In the diagram of a football field, the positions of players are represented by *points*. The yard lines suggest *lines*, and the flat surface of the playing field can be thought of as a *plane*.



In geometry, the words *point*, *line*, and *plane* are **undefined terms**. These words do not have formal definitions, but there is agreement about what they mean.

## TAKE NOTES

When you write new concepts and yellow-highlighted vocabulary in your notebook, be sure to copy all associated diagrams.

## KEY CONCEPT

## For Your Notebook

### Undefined Terms

**Point** A **point** has no dimension. It is represented by a dot.



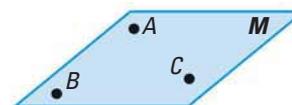
**Line** A **line** has one dimension. It is represented by a line with two arrowheads, but it extends without end.



line  $l$ , line  $AB$  ( $\overleftrightarrow{AB}$ ),  
or line  $BA$  ( $\overleftrightarrow{BA}$ )

Through any two points, there is exactly one line. You can use any two points on a line to name it.

**Plane** A **plane** has two dimensions. It is represented by a shape that looks like a floor or a wall, but it extends without end.



plane  $M$  or plane  $ABC$

Through any three points not on the same line, there is exactly one plane. You can use three points that are not all on the same line to name a plane.

**Collinear points** are points that lie on the same line. **Coplanar points** are points that lie in the same plane.

## EXAMPLE 1 Name points, lines, and planes

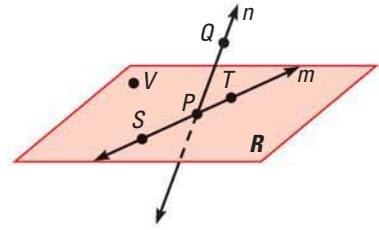
### VISUAL REASONING

There is a line through points  $S$  and  $Q$  that is not shown in the diagram. Try to imagine what plane  $SPQ$  would look like if it were shown.

- Give two other names for  $\overleftrightarrow{PQ}$  and for plane  $R$ .
- Name three points that are collinear. Name four points that are coplanar.

### Solution

- Other names for  $\overleftrightarrow{PQ}$  are  $\overleftrightarrow{QP}$  and line  $n$ . Other names for plane  $R$  are plane  $SVT$  and plane  $PTV$ .
- Points  $S$ ,  $P$ , and  $T$  lie on the same line, so they are collinear. Points  $S$ ,  $P$ ,  $T$ , and  $V$  lie in the same plane, so they are coplanar.



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### GUIDED PRACTICE for Example 1

- Use the diagram in Example 1. Give two other names for  $\overleftrightarrow{ST}$ . Name a point that is *not* coplanar with points  $Q$ ,  $S$ , and  $T$ .

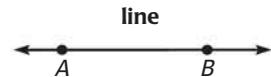
**DEFINED TERMS** In geometry, terms that can be described using known words such as *point* or *line* are called **defined terms**.

### KEY CONCEPT

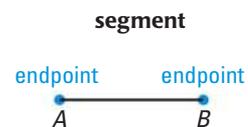
### For Your Notebook

#### Defined Terms: Segments and Rays

Line  $AB$  (written as  $\overleftrightarrow{AB}$ ) and points  $A$  and  $B$  are used here to define the terms below.



**Segment** The **line segment**  $AB$ , or **segment**  $AB$ , (written as  $\overline{AB}$ ) consists of the **endpoints**  $A$  and  $B$  and all points on  $\overleftrightarrow{AB}$  that are between  $A$  and  $B$ . Note that  $\overline{AB}$  can also be named  $\overline{BA}$ .



**Ray** The **ray**  $AB$  (written as  $\overrightarrow{AB}$ ) consists of the endpoint  $A$  and all points on  $\overleftrightarrow{AB}$  that lie on the same side of  $A$  as  $B$ .

Note that  $\overrightarrow{AB}$  and  $\overrightarrow{BA}$  are different rays.



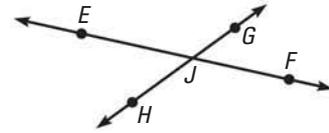
If point  $C$  lies on  $\overleftrightarrow{AB}$  between  $A$  and  $B$ , then  $\overrightarrow{CA}$  and  $\overrightarrow{CB}$  are **opposite rays**.



Segments and rays are collinear if they lie on the same line. So, opposite rays are collinear. Lines, segments, and rays are coplanar if they lie in the same plane.

## EXAMPLE 2 Name segments, rays, and opposite rays

- Give another name for  $\overline{GH}$ .
- Name all rays with endpoint  $J$ . Which of these rays are opposite rays?



### Solution

- Another name for  $\overline{GH}$  is  $\overline{HG}$ .
- The rays with endpoint  $J$  are  $\overrightarrow{JE}$ ,  $\overrightarrow{JG}$ ,  $\overrightarrow{JF}$ , and  $\overrightarrow{JH}$ . The pairs of opposite rays with endpoint  $J$  are  $\overrightarrow{JE}$  and  $\overrightarrow{JF}$ , and  $\overrightarrow{JG}$  and  $\overrightarrow{JH}$ .

### AVOID ERRORS

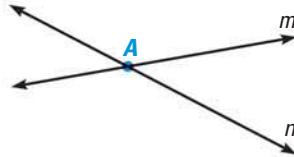
In Example 2,  $\overrightarrow{JG}$  and  $\overrightarrow{JF}$  have a common endpoint, but are not collinear. So they are *not* opposite rays.

## GUIDED PRACTICE for Example 2

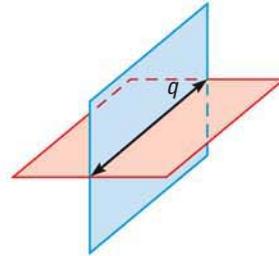
Use the diagram in Example 2.

- Give another name for  $\overline{EF}$ .
- Are  $\overrightarrow{HJ}$  and  $\overrightarrow{JH}$  the same ray? Are  $\overrightarrow{HJ}$  and  $\overrightarrow{HG}$  the same ray? *Explain.*

**INTERSECTIONS** Two or more geometric figures *intersect* if they have one or more points in common. The **intersection** of the figures is the set of points the figures have in common. Some examples of intersections are shown below.



The intersection of two different lines is a point.



The intersection of two different planes is a line.

## EXAMPLE 3 Sketch intersections of lines and planes

- Sketch a plane and a line that is in the plane.
- Sketch a plane and a line that does not intersect the plane.
- Sketch a plane and a line that intersects the plane at a point.

### Solution

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### EXAMPLE 4 Sketch intersections of planes

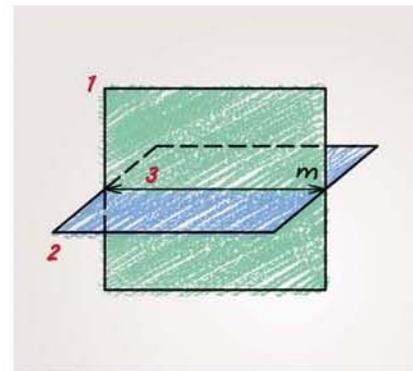
Sketch two planes that intersect in a line.

#### Solution

**STEP 1** Draw a vertical plane. Shade the plane.

**STEP 2** Draw a second plane that is horizontal. Shade this plane a different color. Use dashed lines to show where one plane is hidden.

**STEP 3** Draw the line of intersection.



#### GUIDED PRACTICE for Examples 3 and 4

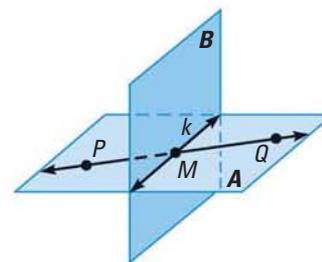
4. Sketch two different lines that intersect a plane at the same point.

Use the diagram at the right.

5. Name the intersection of  $\overleftrightarrow{PQ}$  and line  $k$ .

6. Name the intersection of plane  $A$  and plane  $B$ .

7. Name the intersection of line  $k$  and plane  $A$ .



## 1.1 EXERCISES

#### HOMWORK KEY

**WORKED-OUT SOLUTIONS**  
on p. WS1 for Exs. 15, 19, and 43

**STANDARDIZED TEST PRACTICE**  
Exs. 2, 7, 13, 16, and 43

### SKILL PRACTICE

1. **VOCABULARY** Write in words what each of the following symbols means.

a.  $Q$

b.  $\overline{MN}$

c.  $\overleftrightarrow{ST}$

d.  $\overrightarrow{FG}$

2. **WRITING** Compare collinear points and coplanar points. Are collinear points also coplanar? Are coplanar points also collinear? *Explain.*

#### EXAMPLE 1

on p. 3  
for Exs. 3–7

**NAMING POINTS, LINES, AND PLANES** In Exercises 3–7, use the diagram.

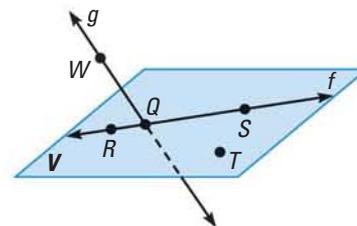
3. Give two other names for  $\overleftrightarrow{WQ}$ .

4. Give another name for plane  $V$ .

5. Name three points that are collinear. Then name a fourth point that is *not* collinear with these three points.

6. Name a point that is *not* coplanar with  $R$ ,  $S$ , and  $T$ .

7. **WRITING** Is point  $W$  coplanar with points  $Q$  and  $R$ ? *Explain.*

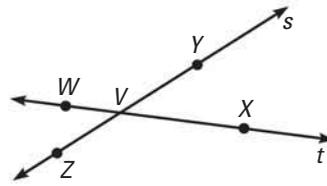


**EXAMPLE 2**

on p. 4  
for Exs. 8–13

**NAMING SEGMENTS AND RAYS** In Exercises 8–12, use the diagram.

8. What is another name for  $\overline{ZY}$ ?
9. Name all rays with endpoint  $V$ .
10. Name two pairs of opposite rays.
11. Give another name for  $\overrightarrow{WV}$ .
12. **ERROR ANALYSIS** A student says that  $\overrightarrow{VW}$  and  $\overrightarrow{VZ}$  are opposite rays because they have the same endpoint. Describe the error.



13. **★ MULTIPLE CHOICE** Which statement about the diagram at the right is true?

- (A)  $A, B,$  and  $C$  are collinear.
- (B)  $C, D, E,$  and  $G$  are coplanar.
- (C)  $B$  lies on  $\overrightarrow{GE}$ .
- (D)  $\overrightarrow{EF}$  and  $\overrightarrow{ED}$  are opposite rays.

**EXAMPLES 3 and 4**

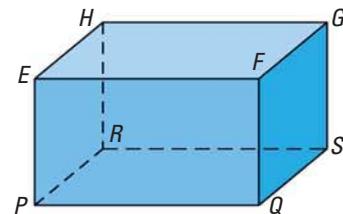
on pp. 4–5  
for Exs. 14–23

**SKETCHING INTERSECTIONS** Sketch the figure described.

14. Three lines that lie in a plane and intersect at one point
15. One line that lies in a plane, and one line that does not lie in the plane
16. **★ MULTIPLE CHOICE** Line  $AB$  and line  $CD$  intersect at point  $E$ . Which of the following are opposite rays?
  - (A)  $\overrightarrow{EC}$  and  $\overrightarrow{ED}$
  - (B)  $\overrightarrow{CE}$  and  $\overrightarrow{DE}$
  - (C)  $\overrightarrow{AB}$  and  $\overrightarrow{BA}$
  - (D)  $\overrightarrow{AE}$  and  $\overrightarrow{BE}$

**READING DIAGRAMMS** In Exercises 17–22, use the diagram at the right.

17. Name the intersection of  $\overrightarrow{PR}$  and  $\overrightarrow{HR}$ .
18. Name the intersection of plane  $EFG$  and plane  $FGS$ .
19. Name the intersection of plane  $PQS$  and plane  $HGS$ .
20. Are points  $P, Q,$  and  $F$  collinear? Are they coplanar?
21. Are points  $P$  and  $G$  collinear? Are they coplanar?
22. Name three planes that intersect at point  $E$ .

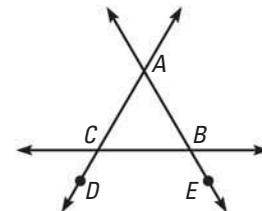


23. **SKETCHING PLANES** Sketch plane  $J$  intersecting plane  $K$ . Then draw a line  $l$  on plane  $J$  that intersects plane  $K$  at a single point.

24. **NAMING RAYS** Name 10 different rays in the diagram at the right. Then name 2 pairs of opposite rays.

25. **SKETCHING** Draw three noncollinear points  $J, K,$  and  $L$ . Sketch  $\overline{JK}$  and add a point  $M$  on  $\overline{JK}$ . Then sketch  $\overrightarrow{ML}$ .

26. **SKETCHING** Draw two points  $P$  and  $Q$ . Then sketch  $\overrightarrow{PQ}$ . Add a point  $R$  on the ray so that  $Q$  is between  $P$  and  $R$ .



**REVIEW  
ALGEBRA**

For help with equations of lines, see p. 878.

**xy ALGEBRA** In Exercises 27–32, you are given an equation of a line and a point. Use substitution to determine whether the point is on the line.

27.  $y = x - 4$ ;  $A(5, 1)$

28.  $y = x + 1$ ;  $A(1, 0)$

29.  $y = 3x + 4$ ;  $A(7, 1)$

30.  $y = 4x + 2$ ;  $A(1, 6)$

31.  $y = 3x - 2$ ;  $A(-1, -5)$

32.  $y = -2x + 8$ ;  $A(-4, 0)$

**GRAPHING** Graph the inequality on a number line. Tell whether the graph is a *segment*, a *ray* or *rays*, a *point*, or a *line*.

33.  $x \leq 3$

34.  $x \geq -4$

35.  $-7 \leq x \leq 4$

36.  $x \geq 5$  or  $x \leq -2$

37.  $x \geq -1$  or  $x \leq 5$

38.  $|x| \leq 0$

39. **CHALLENGE** Tell whether each of the following situations involving three planes is possible. If a situation is possible, make a sketch.

- a. None of the three planes intersect.
- b. The three planes intersect in one line.
- c. The three planes intersect in one point.
- d. Two planes do not intersect. The third plane intersects the other two.
- e. Exactly two planes intersect. The third plane does not intersect the other two.

**PROBLEM SOLVING**

**EXAMPLE 3**

on p. 4  
for Exs. 40–42

**EVERYDAY INTERSECTIONS** What kind of geometric intersection does the photograph suggest?



43. **★ SHORT RESPONSE** Explain why a four-legged table may rock from side to side even if the floor is level. Would a three-legged table on the same level floor rock from side to side? Why or why not?

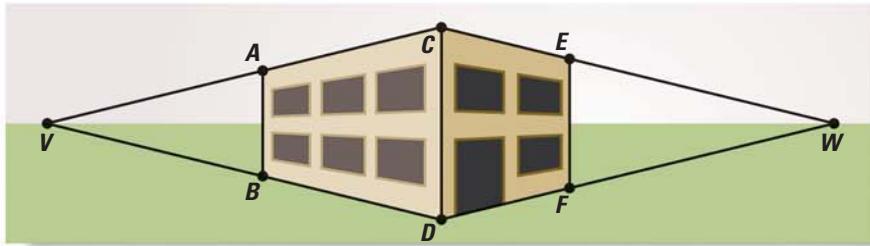
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44. **SURVEYING** A surveying instrument is placed on a tripod. The tripod has three legs whose lengths can be adjusted.
- a. When the tripod is sitting on a level surface, are the tips of the legs coplanar?
  - b. Suppose the tripod is used on a sloping surface. The length of each leg is adjusted so that the base of the surveying instrument is level with the horizon. Are the tips of the legs coplanar? *Explain.*

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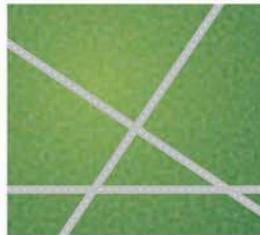
45. **MULTI-STEP PROBLEM** In a *perspective drawing*, lines that do not intersect in real life are represented by lines that appear to intersect at a point far away on the horizon. This point is called a *vanishing point*. The diagram shows a drawing of a house with two vanishing points.



- Trace the black line segments in the drawing. Using lightly dashed lines, join points  $A$  and  $B$  to the vanishing point  $W$ . Join points  $E$  and  $F$  to the vanishing point  $V$ .
  - Label the intersection of  $\overleftrightarrow{EV}$  and  $\overleftrightarrow{AW}$  as  $G$ . Label the intersection of  $\overleftrightarrow{FV}$  and  $\overleftrightarrow{BW}$  as  $H$ .
  - Using heavy dashed lines, draw the hidden edges of the house:  $\overline{AG}$ ,  $\overline{EG}$ ,  $\overline{BH}$ ,  $\overline{FH}$ , and  $\overline{GH}$ .
46. **CHALLENGE** Each street in a particular town intersects every existing street exactly one time. Only two streets pass through each intersection.



2 streets



3 streets



4 streets

- A traffic light is needed at each intersection. How many traffic lights are needed if there are 5 streets in the town? 6 streets?
- Describe a pattern you can use to find the number of additional traffic lights that are needed each time a street is added to the town.

## MIXED REVIEW

Find the difference. (p. 869)

47.  $-15 - 9$

48.  $6 - 10$

49.  $-25 - (-12)$

50.  $13 - 20$

51.  $16 - (-4)$

52.  $-5 - 15$

### PREVIEW

Prepare for  
Lesson 1.2  
in Exs. 53–58.

Evaluate the expression. (p. 870)

53.  $5 \cdot |-2 + 1|$

54.  $|-8 + 7| - 6$

55.  $-7 \cdot |8 - 10|$

Plot the point in a coordinate plane. (p. 878)

56.  $A(2, 4)$

57.  $B(-3, 6)$

58.  $E(6, 7.5)$